# **Experimental Thermodynamics (30 common techniques)**

Surfaces Gas Adsorption Contact Angle Zeta Potential X-ray and Neutron Reflectivity Phase Structure Light, X-ray, Neutron Scattering
Osmotic Compressibility
OM, SEM, TEM, AFM XRD, NPD Chemical Methods

# Calorimetry

Thermal analysis Calorimetry

Differential Scanning Calorimetry Modulated DSC Microcalorimetry Differential Thermal Analysis Thermal Gravimetric Analysis Bomb Calorimetry/Combustion Calorimetry

# Calorimetry

How to build a scanning calorimeter

What is needed? One or Two Adiabatic/Isolated Cells Thermocouples, T Heating rate, dQ/dt Mass, m

#### dT/dQ is measured in the DTA

#### dQ/dT is measured in the DSC

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Simplest approach and useful for very low or very high temperatures is differential thermal analysis DTA

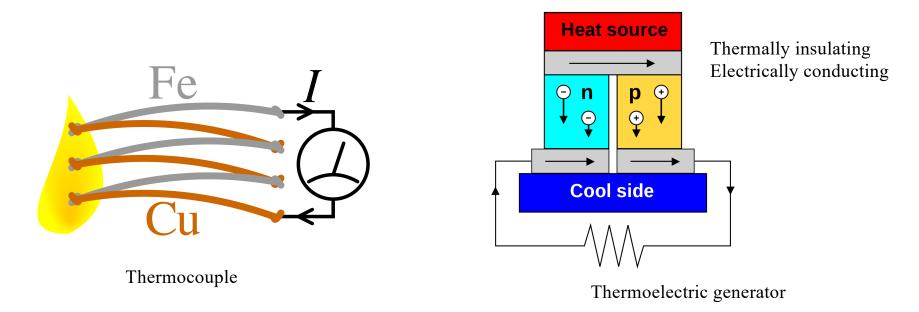
DTA is a simple design for difficult environments

Two cells heated at same rate and the difference in temperature is recorded

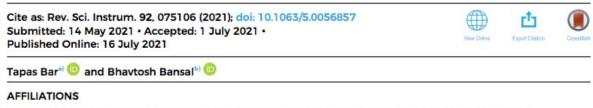
Differences in heat capacity and latent heats create differences in temperatures through transitions.

# Measure the Temperature Seebeck Effect: Thermocouple

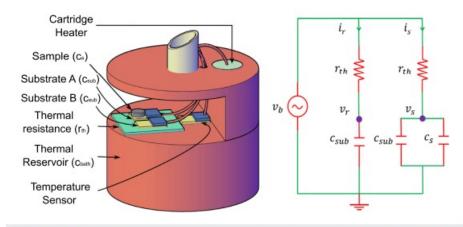
Electrons (or holes) flow from the hot side where they have high kinetic energy to the cold side where they have less kinetic energy. They will spend more time in the cold side, something like condensing in the cold side. This effect is different in magnitude for different metals or semiconductors. The difference in potential at the cold side between two metals is proportional to the temperature. (Similar to thermophoretic sampling.)



# Absolute calibration of the latent heat of transition using differential thermal analysis



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**FIG. 1.** (Left) Schematic of the calorimeter. The sample is mounted on substrate A, and the other nearly identical Pt-100 (substrate B) serves as the reference. An external temperature controller controls the temperature of the thermal reservoir through a temperature sensor and a cartridge heater, which is placed inside the thermal bath. (Right) Equivalent electrical circuit of the calorimeter based on analogy between Biot–Fourier and Ohm's law.

Cryostat Use liquid He or a He refrigerator 4.2K boiling point



## Calorimetry

 $dQ/dt = C_p dT/dt + \Delta H_{transitions}$ 

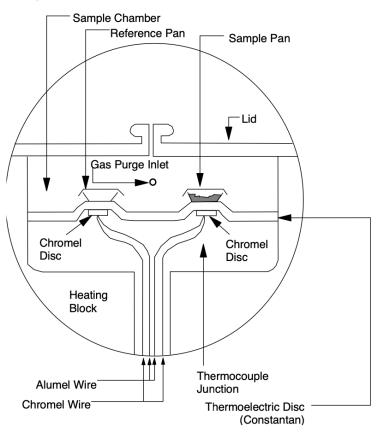
$$\begin{split} \Delta Q &= C_p \left( T_f T_i \right) + \Delta H_{transitions} \\ T_f &= T_i + (\Delta Q - \Delta H_{transitions}) / C_p \\ \Delta Q &= (dQ/dt) t \end{split}$$

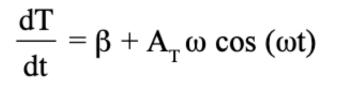
dT/dQ is measured in the DTA dQ/dt = (dT/dt)/(dT/dQ)

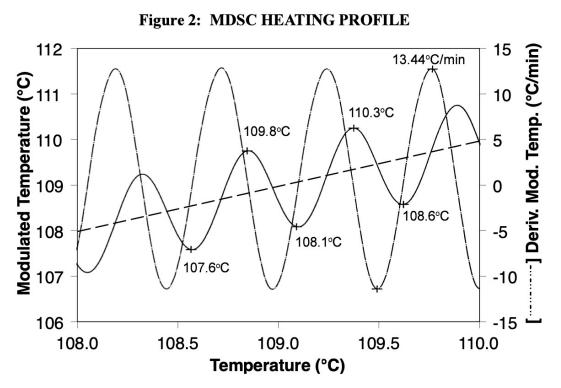
dQ/dT is measured in the DSC dQ/dt = (dQ/dT) (dT/dt)

# **Modulated DSC**

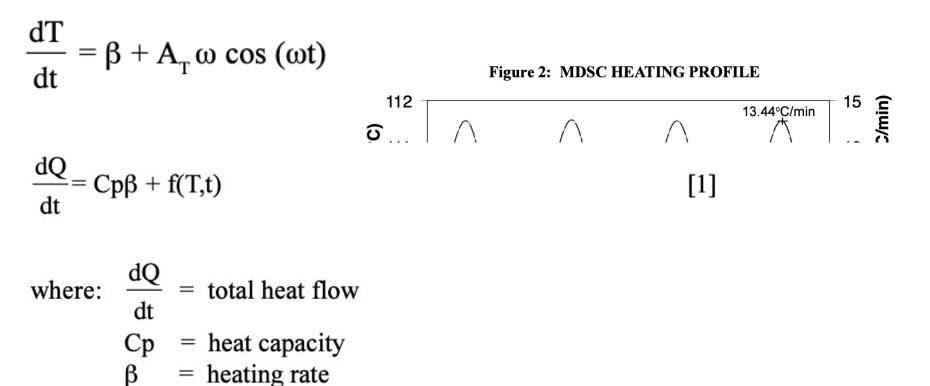
#### Figure 1: HEAT FLUX DSC SCHEMATIC







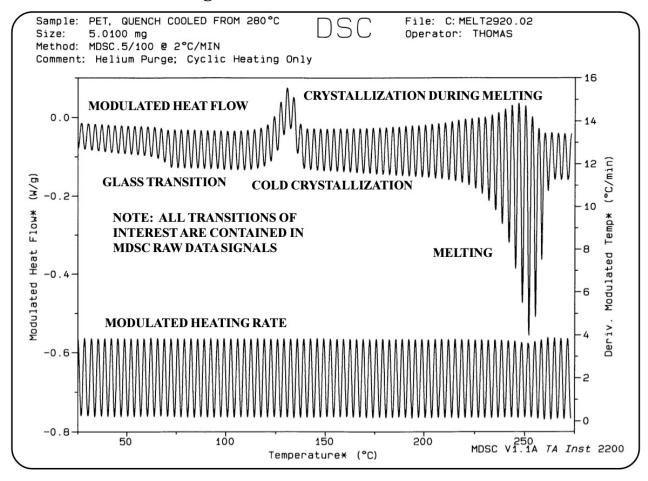
In the example shown in Figure 2, the underlying heating rate is  $1^{\circ}$ C/minute, the modulation period is 30 seconds, and the modulation amplitude is  $\pm 1^{\circ}$ C. This set of conditions results in a sinusoidal heating profile where the instantaneous heating rate varies between  $\pm 13.44^{\circ}$ C/minute and  $\pm 11.54^{\circ}$ C/minute (i.e., cooling occurs during a portion of the modulation). Although the actual sample temperature changes in a sinusoidal fashion during this process (Figure 3), the analyzed signals are ultimately plotted versus the linear average temperature which is calculated from the average value as measured by the sample thermocouple (essentially the dashed line in Figure 2). [Note: As in conventional DSC, MDSC can also be run in a cooling rather than heating mode.]



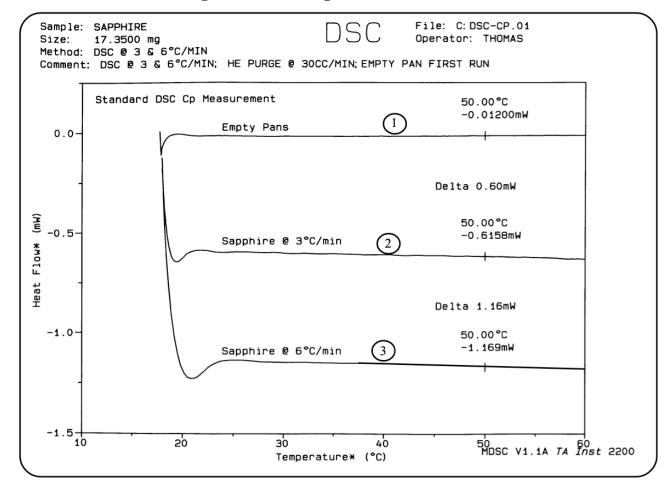
f(T,t) = heat flow from kinetic (absolute temperature and time dependent) processes

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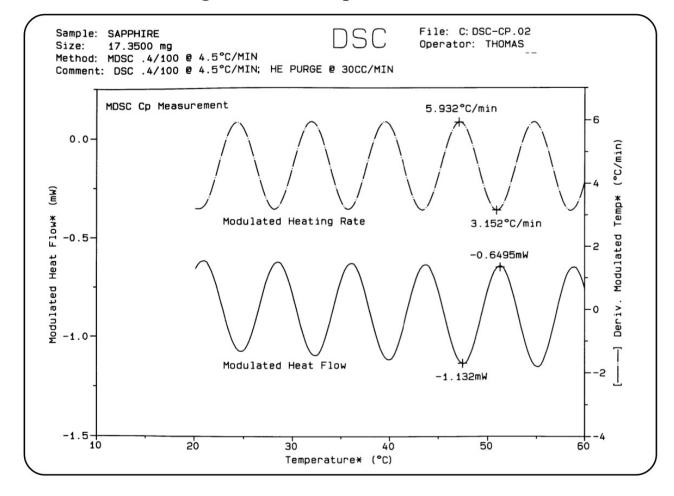
#### Figure 7: MDSC RAW SIGNALS



#### Figure 8: DSC Cp MEASUREMENT



#### Figure 9: MDSC Cp MEASUREMENT



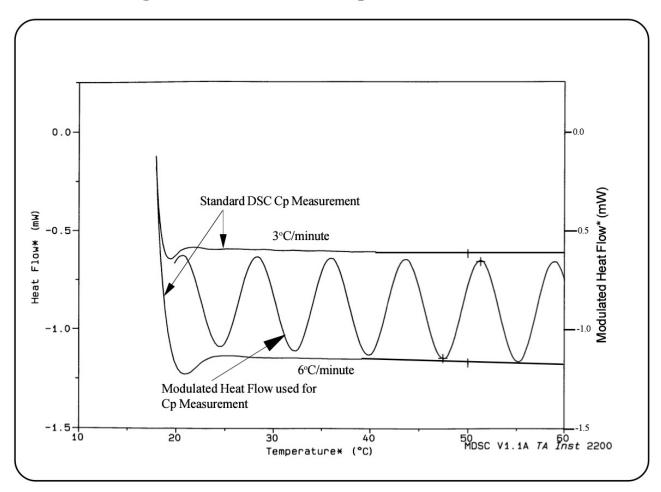
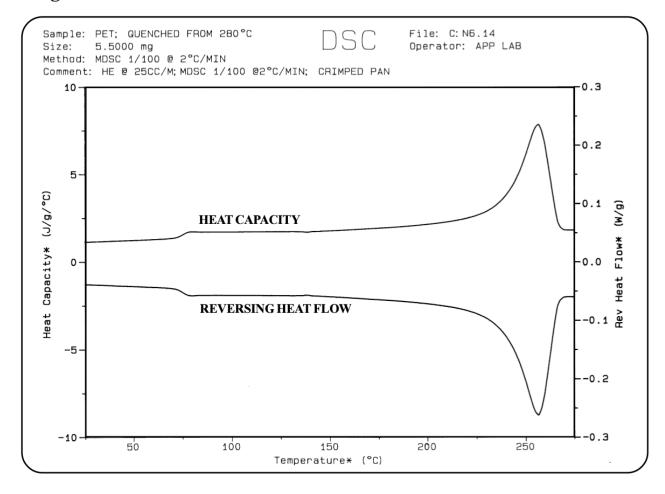
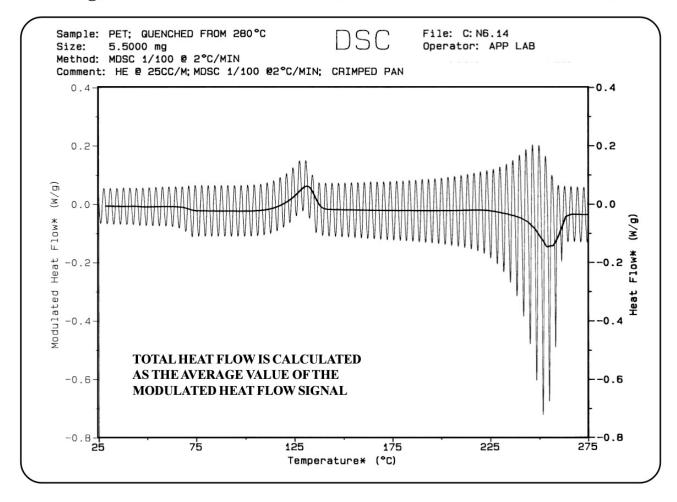


Figure 10: DSC & MDSC Cp MEASUREMENTS

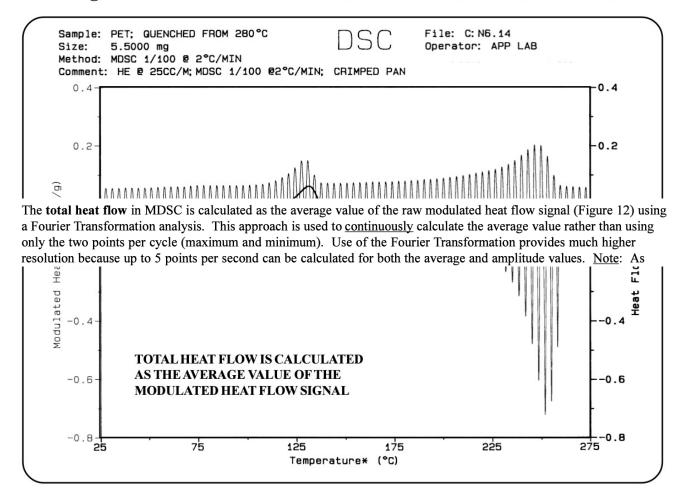
Figure 11: REVERSING HEAT FLOW FROM MDSC RAW SIGNALS

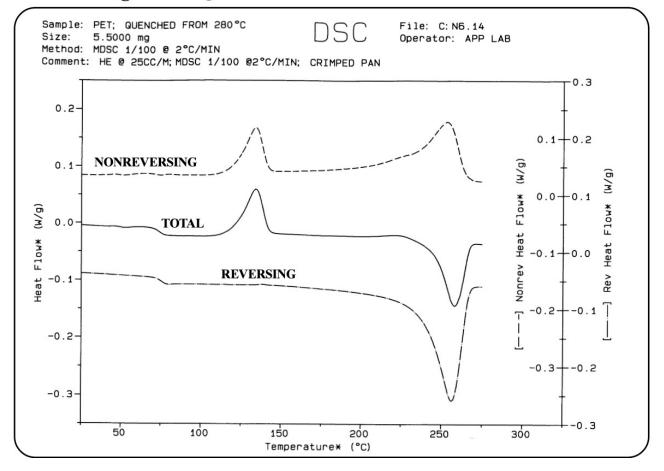


#### Figure 12: TOTAL HEAT FLOW FROM MDSC RAW SIGNALS



#### Figure 12: TOTAL HEAT FLOW FROM MDSC RAW SIGNALS





#### Figure 13: QUENCH COOLED PET - MODULATED DSC

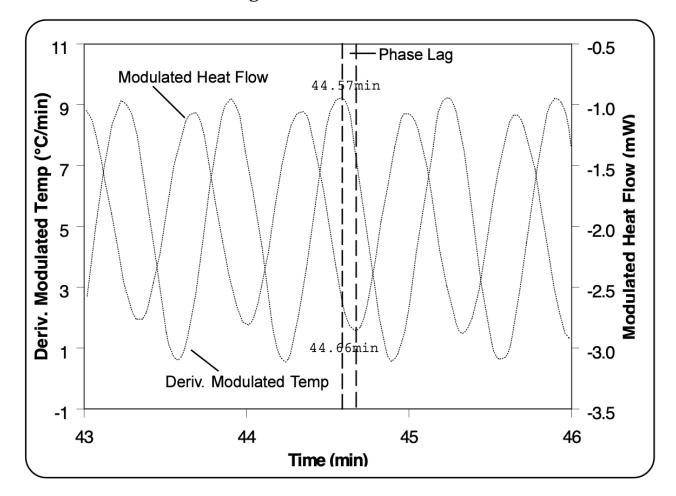
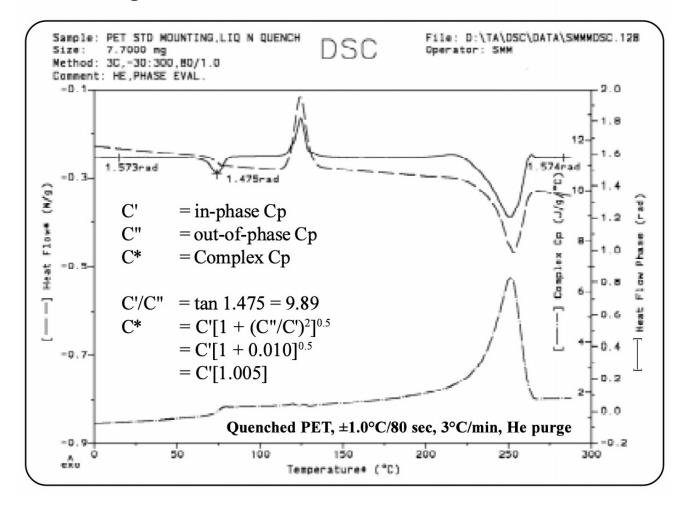


Figure 14: PHASE LAG

#### Figure 15: HEAT FLOW PHASE CONTRIBUTION



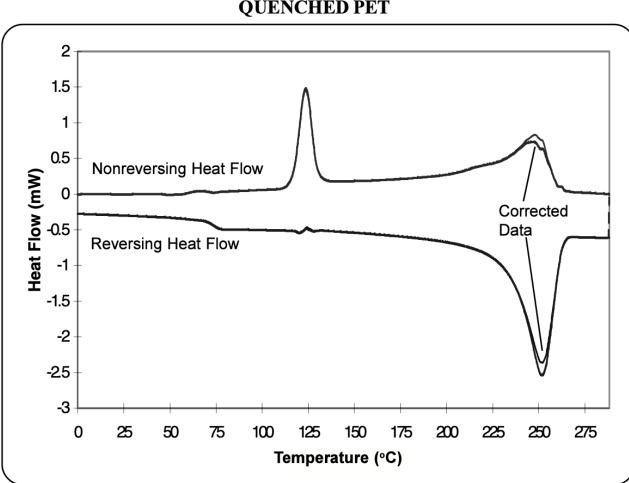
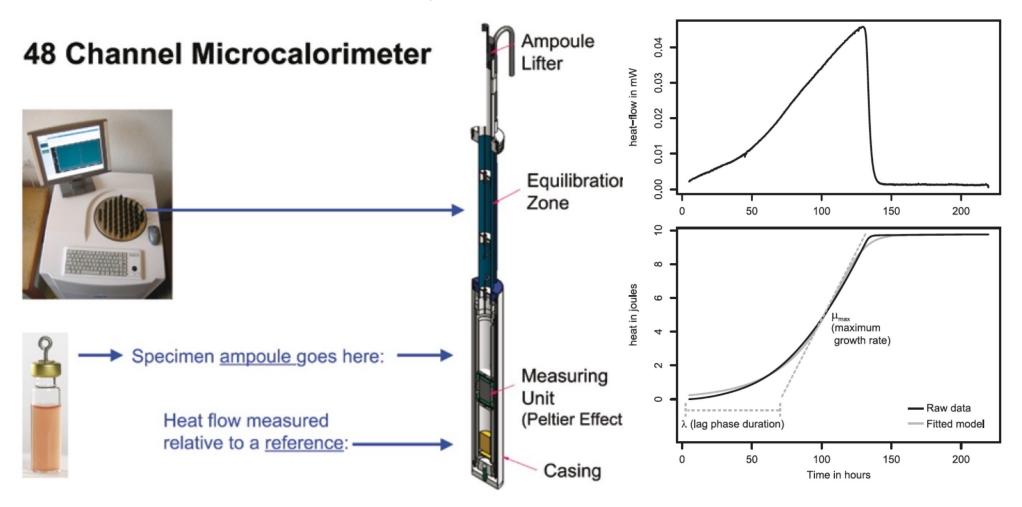
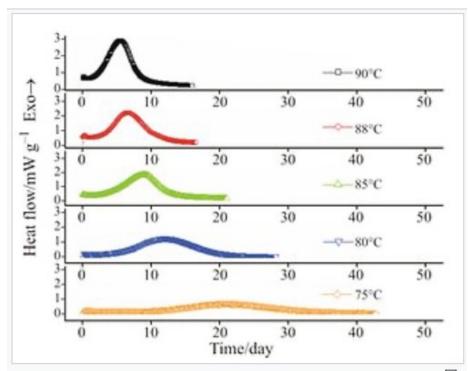


Figure 16: PHASE-CORRECTED HEAT FLOW SIGNALS QUENCHED PET

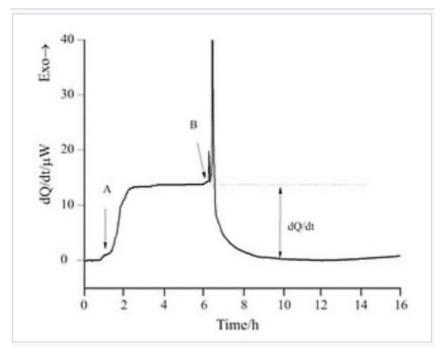
Micro Calorimetry (isothermal shown)



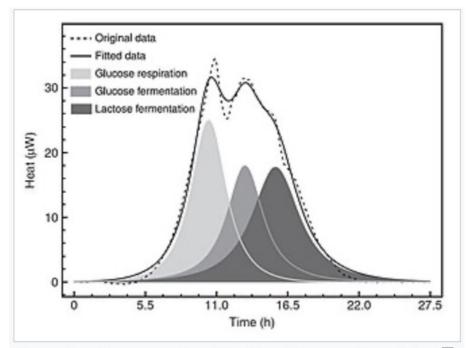


Heat flow vs. time for the thermal decomposition of 80 mass% CHP (cumene hydroperoxide) at a series of temperatures. CHP is an industrial chemical intermediate and polymerization initiator which is a documented fire and explosion hazard. According to the authors, neither differential scanning calorimetry or adiabatic calorimetry was sensitive enough to capture these data (from Chen et al. 2008 with publisher permission).





Heat flow vs. time for the treatment of fibroblasts in culture in a stirred stainless steel ampoule. A = introduction of the ampoule into the measurement position, with metabolic heat flow then reaching an equilibrium level. B = injection of sodium dodecyl sulfate (SDS) which produced sharp heat flow peaks related to exothermic diluton of the SDS and lysis of the fibroblasts. After lysis, the heat flow rate returned near zero since fibroblast metabolism had ceased. dQ/dt = the metabolic heat flow of the fibroblasts in culture (from Liu, et al. 2007 with publisher permission). Fig. 5



Example of how growth-related heat flow vs. time data from bacteria in culture in a given medium in a sealed ampoule reflect the sequence of metabolic activities taking place. The bacteria move on to consuming less efficient carbon sources as more efficient sources are depleted. Deconvolution of the data yielded the peaks shown which can be assigned to the metabolic modes shown. This sequence for the *E. coli* bacteria employed is well known in the field of microbiology (from Braissant et al. 2010 with publisher permission). Fig.6

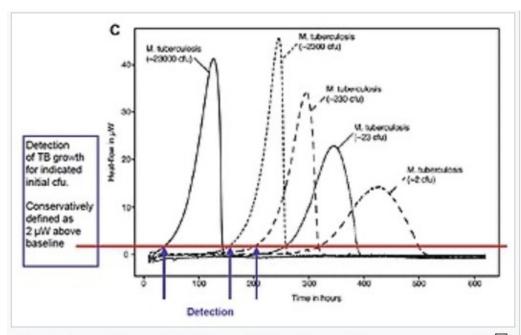


Illustration of how IMC time of detection of the presence of  $\Box$  bacteria depends on the initial number of bacteria present (CFU), the sensitivity of the instrument and the level of heat flow above baseline that is selected as indicating bacterial growth. CFU = colony forming unit. (adapted from Braissant et al. 2010 with publisher permission). Fig.7

# Thermogravimetric Analysis (TGA)



# **Thermogravimetric Analysis (TGA)**

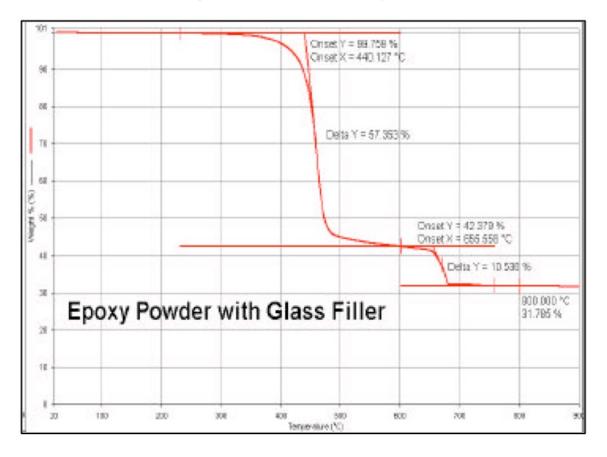


Figure 3. TGA results for epoxy-glass powder

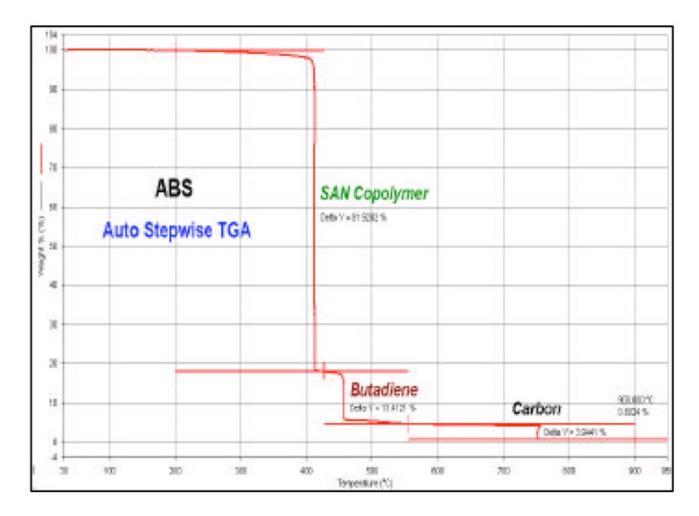


Figure 5. Auto Stepwise TGA results for ABS showing separation of SAN and butadiene components

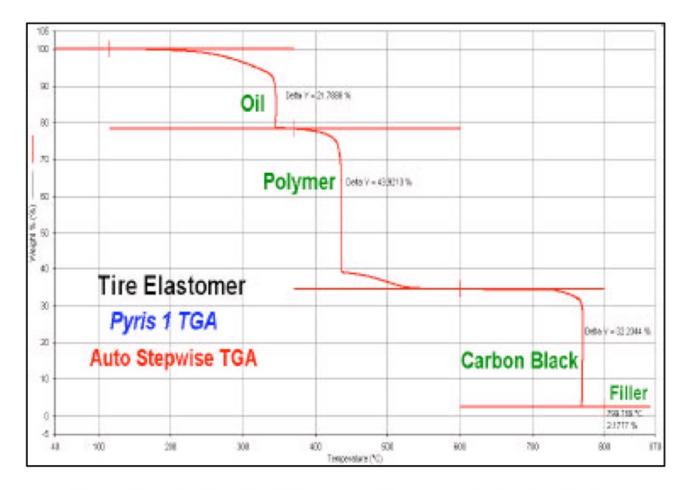


Figure 6. Auto Stepwise TGA compositional results for tire elastomer showing separation of oil, polymer, carbon black and filler

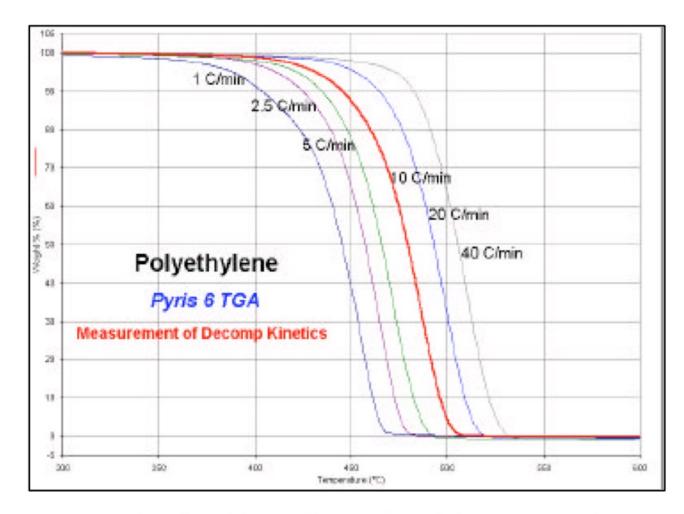
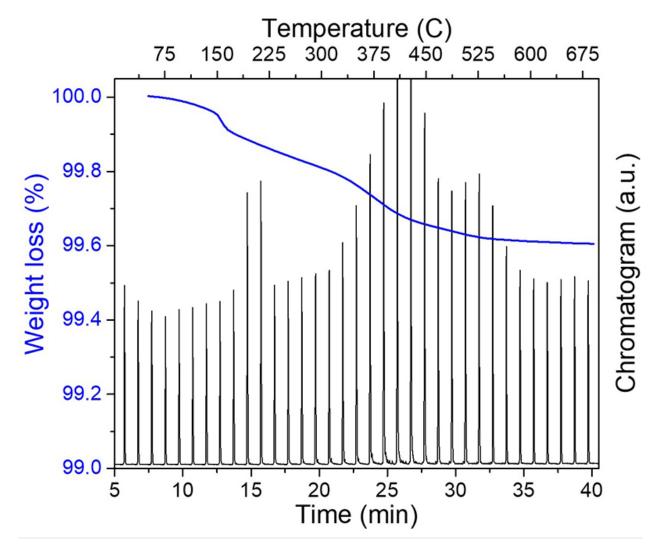


Figure 8. Effect of heating heat on thermal decomposition of polyethylene



# TGA/MS GC IR Raman Etc.

Example of TGA coupled with GC-MS showing the identification of different ions released by the material as a function of temperature

# **Membrane Osmometry**

In an ideally dilute solution, van 't Hoff's law of osmotic pressure can be used to calculate  $M_n$  from osmotic pressure.<sup>[1]</sup>

$$\lim_{c o 0} \left( rac{\Pi}{c} 
ight) = rac{RT}{M_n}$$

 $M_n$ , number average molecular weight, mass/mole

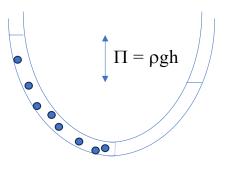
R, gas constant

- T, absolute temperature, typically Kelvin
- c, concentration of polymer, mass/volume
- $\Pi$ , osmotic pressure

$$rac{\pi}{c} = RT\left(rac{1}{M_{\mathtt{a}}} + A_2 c + \cdots
ight)$$

$$A_2 = \frac{1}{M^2} \left( b - \frac{a}{RT} \right)$$

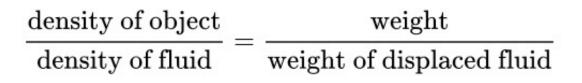
Van der Waals b = Excluded volume a = attractive potential



Van der Waals Equation  $P = \Pi$ 

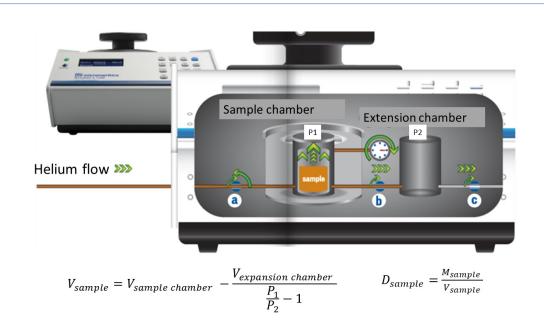
$$P=rac{RT}{V-b}-rac{a}{V^2}$$

# **Archimedes Method for Density**

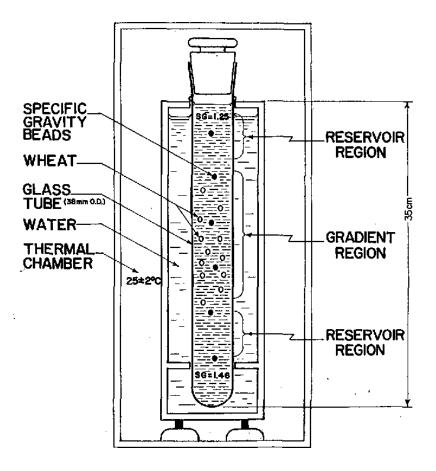




Helium density Boyle's Law  $(P_1V_1 = P_2V_2)$ Measure pressure change to get volume Weigh sample "Open pore" density







# **Density Gradient Column**

# Mercury Dilatometry for Thermal Expansion Coefficient, $\alpha$

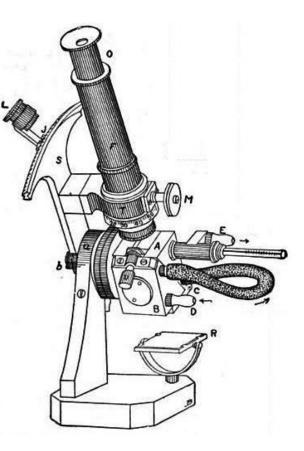
$$\label{eq:alpha} \alpha = \frac{1}{V} \left( \frac{\partial V}{\partial T} \right)_{p,N}$$

### **Abbe Refractometer**

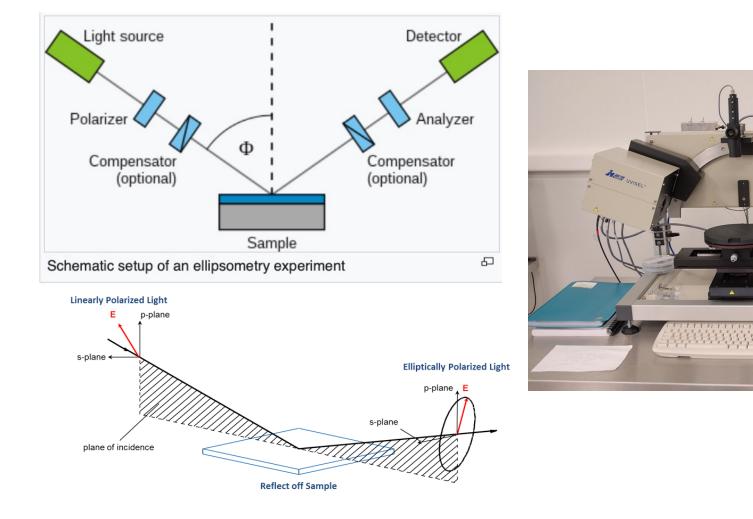
sion of free volume above  $T_g$ . Under the assumption of a spherical molecule, the density  $\rho$  can be related to the index of refraction *n* by using the Lorentz– Lorenz equation,

$$\frac{(n^2 - 1)}{(n^2 + 2)} = \rho C \tag{2}$$

where C is the specific refraction, which depends on the polarizability of the molecules (temperature independent).<sup>19</sup> Equation (2) results in a monotonically decreasing index of refraction with decreasing density.



 $n = \frac{\mathrm{c}}{v}.$ 



## Index (and thickness) of thin films Ellipsometer

The illustration to the right represents a generic volumetric physical adsorption analyzer in its most elementary form. The critical components are:

- 1) Analysis manifold of accurately known volume and temperature
- 2) Vacuum system with valve to manifold
- Source of adsorptive gas (typically, N<sub>2</sub>) with valve to manifold
- 4) Pressure transducer and temperature sensor
- Means for recording the signal from the transducer and temperature sensor
- 6) A sample tube of precisely known free or void-space
- 7) Sample tube connected to analysis manifold
- Means to reduce the temperature of the sample when required, (typically to liquid nitrogen (LN<sub>2</sub>) temperature).

#### Preparation

The adsorptive gas supply valve (3) is closed and the vacuum (2) and sample (7) valves are open allowing the manifold and sample tube to be evacuated. The sample tube is not in the cold bath, so the sample is at ambient temperature.

When the necessary vacuum is achieved, valves 2 and 7 close and the cold bath is raised, cooling the sample to the analysis temperature.

#### **Charging the Manifold**

Valve 3 is opened momentarily to charge the manifold to a pressure  $(P_m)$  slightly above vacuum, preparing the instrument to dispense a dose of adsorptive onto the sample. The quantity of gas  $(n_m)$  in the manifold can be determined from the universal gas law

$$n_m = \frac{P_m V_m}{RT}$$

## Surfaces: Gas Adsorption

#### Dosing

Valve 7 is opened allowing some of the gas to enter the sample tube.

#### Equilibration

Some quantity of gas  $(n_{ads})$  will be adsorbed by the sample and removed from the gas phase. Pressure is monitored until it stabilizes, indicating adsorption has equilibrated. The equilibration pressure (P\_) is recorded.

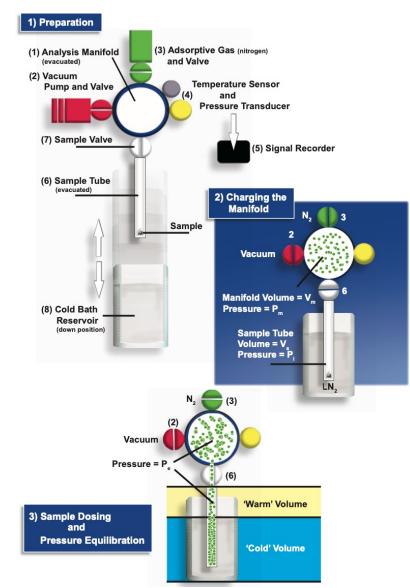
#### **Quantity Adsorbed**

The quantity of gas  $(n_e)$  remaining in the combined manifold and sample tube volume  $(V_m + V_s)$  can be calculated from the universal gas law. This is complicated by the vertical temperature profile in the sample tube, one portion essentially being at ambient temperature and another portion being at the temperature of the cold bath typically LN<sub>2</sub>.

The calculation of  $n_e$  is made traceable by a free-space measurement typically performed prior to the analysis and which characterizes the sample tube volume in regard to 'warm' and 'cold' volumes. Once  $n_e$  is determined, the quantity of gas adsorbed by the sample at  $P_e$  is

$$n_{ads} = n_m - n_c$$

This establishes the point on the isotherm  $(P_e, n_{adv})$ . Valve 7 closes and valve 3 opens, and the manifold is charged to a pressure slightly higher than  $P_e$  after which the dosing and isplay a menu n processes are repeated.



### **Quantity Adsorbed**

The quantity of gas (n,) remaining in the combined manifold and sample tube volume  $(V_m + V_s)$  can be calculated from the universal gas law. This is complicated by the vertical temperature profile in the sample tube, one portion essentially being at ambient temperature and another portion being at the temperature of the cold bath typically LN2.

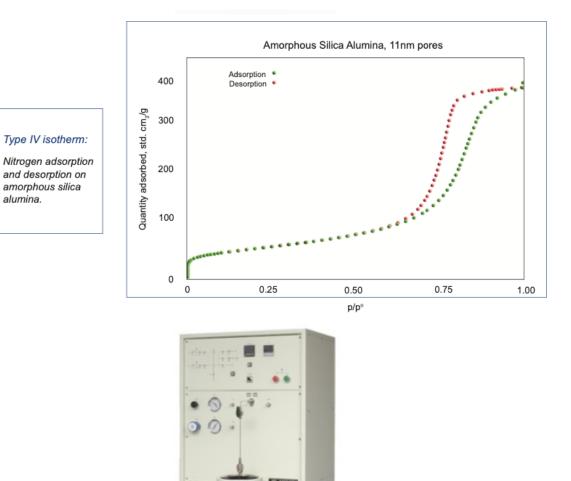
The calculation of n is made traceable by a free-space measurement typically performed prior to the analysis and which characterizes the sample tube volume in regard to 'warm' and 'cold' volumes. Once n is determined, the quantity of gas adsorbed by the sample at P is

alumina.

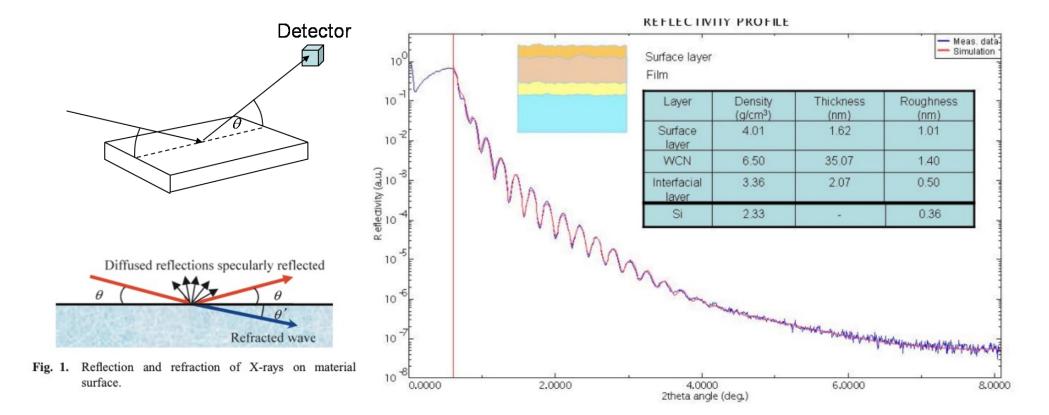
$$n_{ads} = n_m - n_e$$

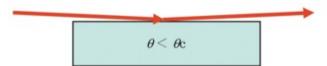
This establishes the point on the isotherm (P, n, ). Valve 7 closes and valve 3 opens, and the manifold is charged to a pressure slightly higher than P after which the dosing and quilibration processes are repeated.

This cycle continues until the analysis pressure is near saturation pressure at which time the complete adsorption isotherm has been developed. The desorption isotherm is measured by a step-wise reduction in pressure until the a low pressure over the sample is achieved. At that point, most of the physically adsorbed molecules will have been desorbed from the surface.

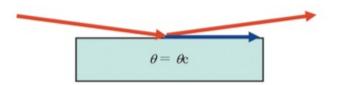


## X-ray and Neutron Reflectivity

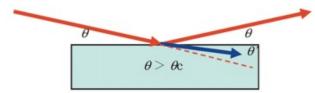




A) Incident angle < Total reflection critical angle</li>
 All incident X-rays are reflected.



B) Incident angle = Total reflection critical angle Incident X-rays propagate along the sample surface.



- C) Incident angle > Total reflection critical angle
   Incident X-rays penetrate into the material by refraction
  - Fig. 3. Reflection and refraction of X-rays at material surface with the changes in the grazing angle.

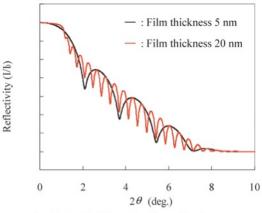


Fig. 4. Reflectivity of Au film on Si substrate.

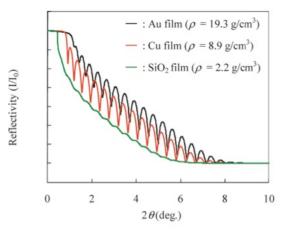


Fig. 5. X-ray reflectivity curves of Au, Cu and SiO<sub>2</sub> film on Si substrates (film thickness is 20 nm).

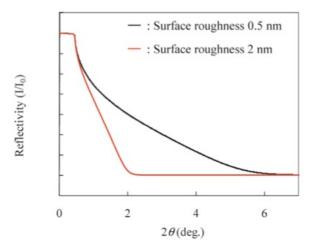


Fig. 6. X-ray reflectivity curves of Si substrates with two different values of surface roughness.

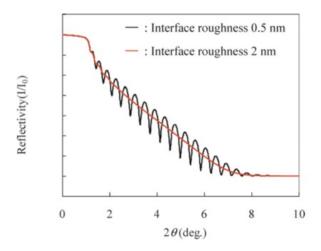


Fig. 7. X-ray reflectivity of Si substrate differences with interface roughness (Film thickness is 20 nm).

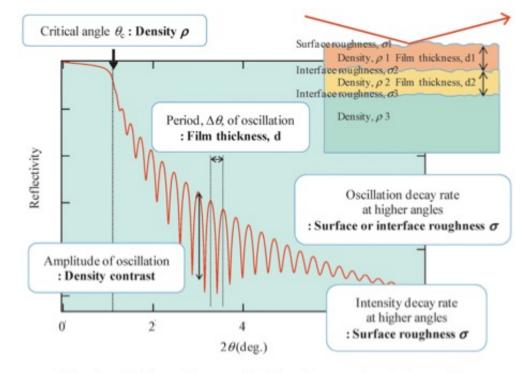
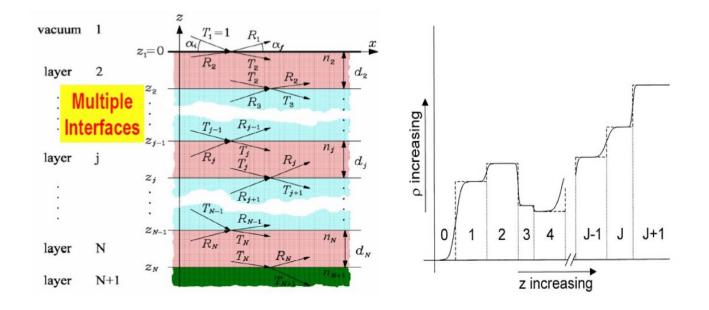
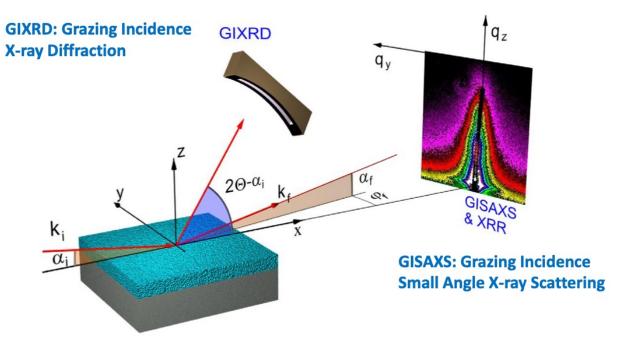


Fig. 8. Information provided by X-ray reflectivity profile.

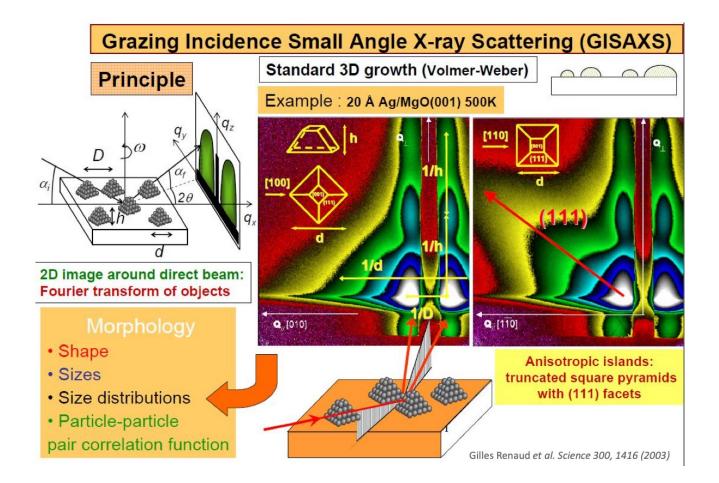
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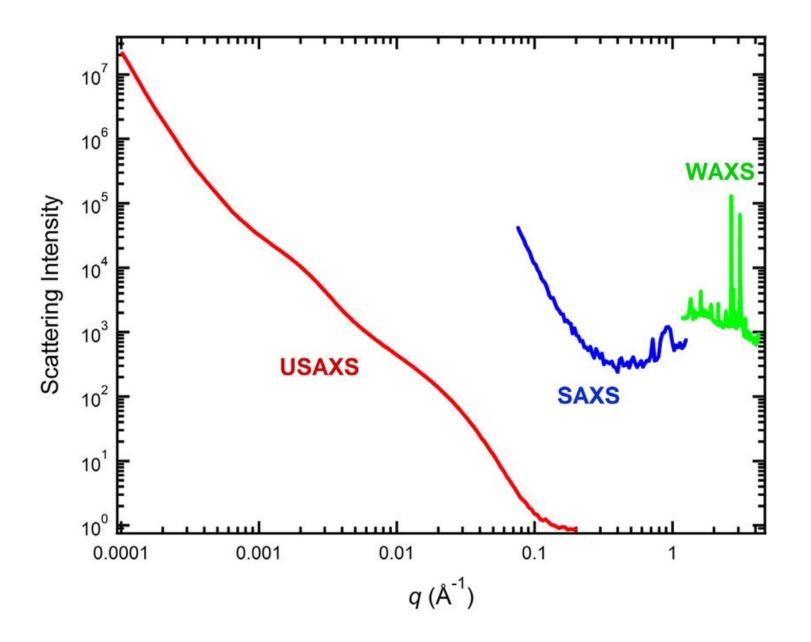
# **Reflectivity from Multiple Layers**

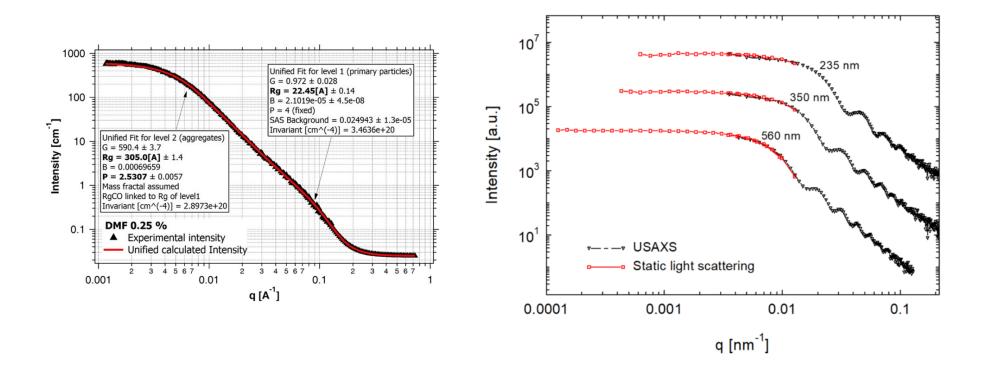




In GISAXS, the angle  $\alpha_i$  is very small (<0.5°) for GISAXS, X-ray penetrates the sample and reflection is very strong, beam stopper is required to protect detector. In our experiment,  $\alpha_i = 1.8^\circ$ , beam intensity is reduced dramatically, no stopper.



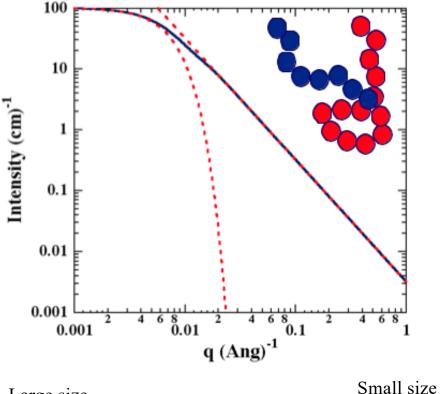




### Small-Angle Light, Neutron, and X-ray Scattering for Osmotic Compressibility

"Thermodynamic Limit"

At large sizes contrast arises from thermally driven fluctuations in density that are opposed by the osmotic compressibility,  $(d\rho/dP)_T$  The observed intensity  $I(q=>0) \sim kT/(d\rho/dP)_T$ Here P is  $\Pi$  the osmotic pressure which can be expressed using the virial expansion so that the first derivative is the second virial coefficient A<sub>2</sub>. Low-q scattering can measure the thermodynamic interaction of particles.



Large size ( $2\pi/0.001$ ) Å = 600 nm Small size ( $2\pi/1$ ) Å = 0.6 nm

